

LESSON 3: EQUATIONS OF LINES

- Objectives:
1. To define the slope of a line
 2. To know the various forms of equations of lines
 3. To find the slope of a line perpendicular to a given line

Slope of a Line

$$\text{Slope} = m = \text{rise} = \frac{\text{rise}}{\text{run}} = \frac{\text{change in } y}{\text{change in } x} = \frac{\Delta y}{\Delta x} = \frac{y_2 - y_1}{x_2 - x_1}$$

$$\text{Parallel Lines } m_1 = m_2$$

$$\text{Perpendicular Lines } m_1 \cdot m_2 = -1$$

Equations of Lines

General $Ax + By + C = 0$

Slope-intercept..... $y = mx + b$

Point-slope $y - y_1 = m(x - x_1)$

Modified Point-slope $y = m(x - x_1) + y_1$

Horizontal $y = b$

Vertical..... $x = a$

Intercept Form $\frac{x}{a} + \frac{y}{b} = 1$, for $x\text{-int} = a$ and $y\text{-int} = b$

Problems

1. Find the equation of the line that passes through the point $(-2, -3)$ and is perpendicular to the line given by $2x - 4y = 5$.
2. Find the equation of the line that passes through points $(-2, 5)$ and $(-2, -11)$.
3. Find the equation of the circle through the points $A(4, 3)$, $B(-2, -5)$, and $C(5, 2)$.